PERFORMANCE EVALUATION OF LTE NETWORK USING MAXIMUM FLOW ALGORITHM

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ABSTRACT

In this paper, we propose a new traffic flow model of the Long Term Evaluation (LTE) network for the Evolved Universal Terrestrial Radio Access Network (E-UTRAN). Here only one Evolve Node B (eNB) nearest to the Mobility Management Entity (MME) and Serving Gateway (S-GW) will use the S1 link to bridge the E-UTRAN and Evolved Packet Core (EPC). All the eNBs of a tracking area will be connected to each other by the X2 link. Determination of capacity of a links of such a network is a challenging job since each node offers its own traffic and at the same time conveys traffic of other nodes. In this paper, we apply maximum flow algorithm including superposition theorem to solve the traffic flow of radio network. Using the total flow per subcarrier, a new traffic model is also developed in the paper. The relation among the traffic parameters: 'blocking probability', 'offered traffic', 'instantaneous capacity', 'average holding time', and 'number of users' are shown graphically under both QPSK and 16-QAM. The concept of the network will be helpful to improve the SINR of the received signal ofeNBslocated long distance relative to MME/S-GW.

KEYWORDS

Aggregate offered traffic, blocking probability, traffic channel, weighted graph and RB.

1. INTRODUCTION

Traffic analysis of the LTE network is found in recent research works and few of them which are relevant to the paper is considered here. In [1] analytical model of LTE traffic is shown based on the Markov chain then the traffic model is combined with fading parameters (Rayleigh fading with MIMO) of a wireless link. The probability of forced termination and blocking of calls are plotted against call arrival rate and the number of channels. A similar analysis is found in [2], where M/M/m/m/c state transition is used to measure the blocking probability of the LTE network. An algorithm called, 'Extended Erlang B formula' is proposed to evaluate the performance of the network and final 'blocking probability' is plotted against the number of iteration of the algorithm. In [3] soft frequency reuse (SFR) performance of LTE is done by simulation, where the throughput of a cell is plotted against traffic load and cell radius. In [4] authors compare different algorithms pertinent to prioritizing traffic on LTE mobile network. Four traffic parameters: throughput, delay, packet delivery ratio and packet loss ratio are considered to compare the Quality of Service (QoS) of the network and results are shown graphically. In [5] only one traffic parameter called jitter (delay difference) is related with resource block (RB) assignment of LTE network under real time multimedia traffic. In performance evaluation they consider High Definition (HD) video stream of uplink (UE to eNB) using a simulation under Network Simulator (NS3). In [6] authors mainly focus on growth in

DOI: 10.5121/ijcsit.2020.12406

mobile data traffic and enhancement of capacity of LTE network. Application of unlicensed spectrum in LTE network is considered as the best way to increase the data rate of WAN. The pros and cons of existing carried traffic improvement methods: coexistence between LTE-U and Wi-Fi, Dynamic Channel Selection, Listen Before Talk (LBT) traffic, Traffic Offloading, Resource Allocation etc. are discussed with some future issue. In [7] authors proposed traffic model of LTE-WLAN network. The state transition chain of Bianchi model is modified, where the probability of idle and busy state of the network is applied in a different way. Taking typical traffic and wireless link parameters, authors plot the probability of 'transmission of at least one node', 'successful transmission' and 'normalized throughput' against the 'number of nodes'. The impact of size of the 'minimum backoff window' is applied on the graphs of result section, where analytical results are varied by simulation and authors claim high confidence level.

In this paper, we relate the traffic model of LTE with the maximum flow algorithm. Therefore, some works on the maximum flow algorithm and their applications are mentioned in this section. The Ford Fulkerson and Edmonds-Karp algorithm are widely used in the determination of the maximum flow of a system like a computer/communication network, traffic flow, or fluid flow. The solution of the algorithm using C# is available in [8] with its complexity. In [9] authors propose an incremental maximum flow algorithm, where augmenting routing tree is used to reduce the time complexity of the algorithm. The algorithm is applicable in evaluating the capacity of a dynamic network. Another analysis is found in [10], where maximum flow is determined based on a new technique of augmenting path called draining algorithm. The algorithm works better for a near-saturated network but shows computational complexity like a conventional augmenting path for the case of regular flow networks.

Analysing all the papers of this section we found three research gaps:(1) none of above papers deals with accumulation of data traffic of a tracking area of E-UTRAN to an eNB(as a sink) which is nearest to MME/S-GW then high capacity link between that eNB and EPC will carry the combined traffic flow (2) the maximum flow algorithm is applied for the first time in the E-UTRAN region of LTE network (3) the maximum flow algorithm of [11]. If the nearest eNB fails then the second nearest eNB will act as the sink unlike the Radio Network Controller (RNC) of 3G.Objective of above modifications of existing LTE network is to improve the SINR of wireless link between eNB and EPC. In this paper three parameters: simultaneous RB of LTE (as traffic channel), the modulation scheme (QPSK and 16-QAM used in LTE), and Erlangs traffic model are combined with aid of maximum flow algorithm to measure the performance of the network.

The rest of the paper is organized as section 2 deals with the proposed radio network of LTE, its traffic model, and the modified maximum flow algorithm, section 3 provides results based on a theoretical analysis of section 2 and section 4 concludes the entire analysis.

2. System Model

This section gives the theoretical analysis of the proposed traffic model and steps of the maximum flow algorithm (combination with superposition theorem) in the context of the proposed radio network. To make the idea clear, we first introduce the physical architecture of the conventional LTE network and the proposed radio network.

2.1. LTE Network

LTE network has four important features that make the breakthrough of the previous 3G. The features are femtocell deployment, OFDMA-based physical layer access, MIMO, and elimination of radio network controller (RNC) or base station controller (BSC) of the previous generation. To

under standard the traffic model of the paper we first introduce the physical architecture of LTE-A as shown in fig.1, which mainly consists of two parts: E-UTRAN (radio network) and EPC (core switching part). In E-UTRAN, the eNBs are mutualy connected by the X2 link and to EPC by S1 link as found in [12-13]. The outdoor traffic is routed through macro eNB and EPC but indoor traffic is offloaded by the Internet. In this paper, we concentrated on an outdoor traffic model, where a user is connected to MME/S-GW through its nearest macro eNB. An MME serves a large number of eNBs under a tracking area. A user first sends its paging message to MME through its eNB before establishing a connection. The MME verifies the authenticator of the user with the help of a database called, Home Subscriber Server (HSS). After authentication an S1 link is established between eNB and the S-GW. The Serving Gateway (S-GW) route the internal traffic of the network. The Packet Data Network Gateway (P-GW) is responsible for routing traffic of external network under a trusted group of 3GPP where Evolved Packet Data Gateway (ePDG) does the work for the untrusted user group of 3GPP.



Fig.1: Physical architecture of LTE

In this paper, we propose a new radio network of LTE, where eNBs are connected by X2 links like the conventional network, and the entire traffic carried by the eNBs will be accumulated at a node nearest to the MME/S-GW. The nearest node is indicated by n will be connected to the MME/S-GW by a high capacity S1 link as shown in fig.2. The combined traffic of the E-UTRAN is applied to EPC by the high capacity link has the capacity of C. Here all the eNBs can be considered as the sources and the noden where entire traffic is collected can be thought as the sink, hence maximum flow algorithm is applicable for such network.



Fig.2: Universal Terrestrial Radio Access Network (UTRAN) of LTE

2.1. Traffic Model

In fig.2 if the offered traffic of *i*theNB is A_i then the aggregate offered traffic experienced on sink node will be,

$$A = \sum_{i=1}^{n} A_i = \lambda_T t_h \tag{1}$$

Where $\lambda_T \rightarrow \text{arrival}$ rate of resource block (RB) in RB/ms and $t_{he} \rightarrow \text{service}$ time of an RB in ms. We know the duration of an RB is 0.5 ms and the number of symbols in 0.5ms is 7 under normal cyclic prefix (CP). In QPSK each symbol carries 2 bits, therefore the number of bits per RB per subcarrier is $2 \times 7 = 14$ bits.

Now the bit rate/subcarrier =14/0.5 =28Kbps =0.028 Mbps.

The aggregate offered traffic, $A = \lambda_T t_h = 0.5 t_h$

The node *n* is anchored with the core switch hence node *n* is considered as the sink of the maximum flow algorithm as found in [14-15]. The nodes i = 1, 2, 3, ..., n-1 are the sources and we have only one node *n* works as the sink, therefore the Ford-Fulkerson Algorithm in determination maximum flow needs some modification. In this paper, we propose the following modified algorithm where we add the superposition theorem with amaximum flow algorithm.

2.2. Maximum Flow Algorithm with Superposition Theorem

- (a) Determine the weighted graph of the connected eNBs of the tracking area.
- (b) Initialize all the edges with weight W_{ij} between node *i* and *j* with the unit of Mbps.
- (c) Take the node 1 as the source and make all the nodes of the network inactive (simply repeater) and the node *n* works as the sink; provided node *n* is connected to MME/S-GW.
- (d) Determine maximum flow Y_1 from node 1 to n; where the offered data of node 1 is C_1 Mbps.
- (e) Record all the used capacity U_{ij} and remaining capacity R_{ij} of each edge.
- (f) If $Y_1 < C_1$ then enhance the remaining capacity of links to secure $Y_1 \ge C_1$.
- (g) Repeat steps (c) to (e) for the node 2 with offered data rate of C_2 Mbps to secure maximum flow of $Y_2 \ge C_1 + C_2$.
- (h) Repeat steps (c) to (e) to support the aggregate data flow of all sources to sink, $Y = \sum_{i=1}^{m} C_{i}$

Let the total flow is found as *C* Mbps/subcarrier. Since the bit rate/subcarrier of a RB under QPSK is 0.028 Mbps (as found before) therefore the number of RBs carried by the network simultaneously will be, $N = \left| \frac{C}{0.028} \right|$.

Let the field survey provides that each user on an average claims *m* RB per call. If the capacity of the network is *N* RBs then the number of channel of the network will be, $k = \left| \frac{N}{m} \right|$.

Each user on the network generates average of *s* calls/min, *m* RB are used on each call and the duration of a call is t_h min. The offered traffic per user in terms of RB is, $a = (s.m)t_h = smt_h$ The total offered traffic, $A = aM = smt_hM$.

Example-1

Let M = 200, m=3 RB/call/user, $t_h = 1.5$ mins and s = 1/60 min. If the current capacity of the network is 25 RB then find the offered traffic and number of channel.

 $A = smt_h M = (1/60) \times 3 \times (1.5) 200 = 15$ Erls.

The number of channels, $k = \left\lfloor \frac{N}{m} \right\rfloor = \left\lfloor \frac{25}{3} \right\rfloor = 8$

The blocking probability using Erlangs B formula of [16-17],

$$B(A,k) = \frac{\frac{A^{k}}{k!}}{\sum_{i=0}^{k} \frac{A^{i}}{i!}}$$
(2)

If B(A, k) is weighted with the symbol error rate (SER) of QPSK and 16-QAM we get the relation between network traffic and SNR of the link (UE and eNB).

3. RESULTS

In LTE two types of modulation schemes: OPSK and 16-OAM are used. When users are adjacent to eNB then they receive strong SNR and the system use 16-QAM (4 bits/symbol) again when users are at cell boundary experience huge fading then use OPSK scheme (2bits/symbol). Therefore throughput is higher when users are closed to eNB. In the section, we first consider the case of the QPSK scheme. The weighted graph of fig.3 is the interconnected eNBs, where each node corresponds to eNB and the edges are the wireless link among eNBs. Here we assume that each node offers the data of 2Mbps/subcarrier. This is not the typical value of the offered load of the LTE network, we only assume it to verify the profile of traffic parameters. The weight of each edge is the channel capacity (in Mbps) of that link. Here we use nine eNBs and found the maximum flow from the *i*th node to sink node 9 (using Matlab 18) as shown in Table I. We consider, the number of users M = 50, 100 and 200, average RB /call m = 5, average arrival rate per user: (1/60)/min, and the modulation scheme of QPSK. Fig.4(a)-(c) show the variation of 'blocking probability' against 'offered average RB /call' taking 'average holding time' as a parameter. Here blocking probability increases with an increase in 'offered average RB /call', 'number of users', and 'holding time'. The rise of all curves is found exponential and mutually parallel. Actually 'offered average RB /call' m is proportional to offered traffic at the same time inversely proportional to the number of channels hence fig.4 shows the curves equivalent to offered traffic vs. blocking probability (B) of Erlang's model. For all the curves of fig.4, we consider a network of low capacity i.e. C = 2.2 Gbps, therefore the blocking probability is found very high. In a practical network, capacity C is thousands of times higher than the value used for fig.4 hence practical blocking probability is very low.



Fig.3 Equivalent weighted graph of interconnected eNBs of LTE



Number of RB/call (m)

(a) M = 50



Number of RB/call (m)

(b) M = 100



(c) *M* =200

Fig.4 Variation of offered RB/call (m) against blocking probability

The variation of blocking probability against the 'simultaneous capacity of RB' taking 'average holding time' as a parameter is shown in fig.5. Three graphs are shown for m = 2, 3, and 4. The 'simultaneous capacity of RB' is equivalent to the number of channels hence the curves of fig.5 are equivalent to the curve of 'number of channels' vs. blocking probability. The blocking probability decreases with an increase in the 'simultaneous capacity of RB' but reveres relation is found with 'average holding time'. The blocking probability also increases with an increase in m is also visualized from fig.5 (a)-(c).



Number of Simultaneous RB (N)

(a) m = 2



(c) m = 4

Fig.5 Variation of the number of simultaneous RB (N) against blocking probability

Next, we consider a network of higher capacity as shown in fig.6; where we assume that each node offers the data of 4 Mbps/subcarrier. Using the maximum flow algorithm, we got the flow of data from the *i*th node to sink node 9 is shown in table II. Let the number of users is M = 50, 100, and 200 and the capacity C = 9 Gbps. Now our aim is to observe the impact of incrementof capacity from source to sink like before. The blocking probability is found lower than the previous case as shown in fig.7 (a)-(c).

International Journal of Computer Science & Information Technology (IJCSIT) Vol 12, No 4, August 2020



Fig.6 Equivalent weighted graph of interconnected eNBs of LTE of higher capacity



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(c) M = 200

Fig.7 Variation of offered RB/call (m) against blocking probability under QPSK Table-I: Maximum flow per subcarrier

Source	Sink	Maximum flow
		(Mbps/subcarrier)
1		2.2
2		3.3
3		3.3
4	9	2
5		2
6		2.2
7		3.3
8		3.3

Table-II: Maximum flow per subcarrier

Source	Sink	Maximum flow
		(Mbps/subcarrier)
1		9
2		15
3		11
4	9	9
5		4
6		13
7		17
8		18



(a) M = 50



(b) M = 100



(c) M = 200

Fig.8 Variation of RB/call against B under 16-QAM

In 16-QAM the number of simultaneous RB carried by the network becomes, $N = \left\lfloor \frac{C}{0.056} \right\rfloor$ i.e.

half of QPSK. Therefore the performance is deteriorated under 16-QAM visualized from fig. 8. HereN is taken as the number of traffic channels of Erlang's model of the previous section, which is half compared to QPSK but throughput remains the same since each symbol of 16-QAM carries twice the bits of QPSK. Therefore the RR/call i.e. *m* under 16-QAM is just half of QPSK to keep the same throughput hence performance remains the same like fig. 7. If we could relate the traffic model with SNR of link then we could get better performance under 16-QAM at higher SNR.

4. CONCLUSIONS

In this paper, we relate the simultaneous RB, modulation scheme, and traffic parameters to measure the performance of the LTE network. The traffic model used here is M/M/n, in future we will develop M/G/n/K model applicable for RB of both fixed and variable length. Here we consider QPSK and 16-QAM under the awgn scheme. To get a more realistic result we have to consider small scale fading environments like Rayleigh or Nakagami-*m* case. The entire result of the paper is analytical, in the future we will develop a simulation model with fading parameters.

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