

A Novel Approach to Design the Finite Automata to Accept the Palindrome with the Three Input Characters

P. Ezhilarasu¹, J. Prakash¹, N. Krishnaraj², D. Satheesh Kumar¹,
K. Suresh Babu³ and C. Parthasarathy⁴

¹Department of Computer Science and Engineering, Hindusthan College of Engineering and Technology, Coimbatore - 641032, Tamil Nadu, India; prof.p.ezhilarasu@gmail.com, jeevaprakash86@gmail.com, dsatheeshme@gmail.com

²Department of Information Technology, Valliammai Engineering College, Kattankulathur, Chennai - 603203, Tamil Nadu, India; drnkrishnaraj@gmail.com

³Department of Electronics and Communication Engineering, Hindusthan Institute of Technology, Coimbatore - 641032, Tamil Nadu, India; ammaskhicet@gmail.com

⁴Department of Mechatronics Engineering, Hindusthan College of Engineering and Technology, Coimbatore - 641032, Tamil Nadu, India; aruncps3000@gmail.com

Abstract

Background/Objectives: In this paper we discuss that, how Finite Automata can accept the palindrome statically. **Methods/Statistical Analysis:** The formula $3^0 + 3^1 + 3^2 + \dots + 3^n$ used to derive the possible strings. Where 3 represents input character and n represents maximum length of the string. Here the value of n taken as 5. **Findings:** The formula $2 \cdot 3^1 + 2 \cdot 3^2 + 1 \cdot 3^3$ used to derive palindrome from the possible strings. **Application/Improvements:** This method shows the extended use of Finite Automata as compared with the Turing Machine.

Keywords: Finite Automata, Input Characters, Palindrome, String Length, Turing Machine

1. Introduction

Theory of computation defined as computation through the abstract machines. The three primary abstract machines used are Finite Automata Pushdown Automata and Turing Machine. The first two abstract machines moves only in unidirectional. i.e reading strings from the left most to the right most. They cannot perform the movement from the right to left. To overcome this problem the Turing machine used. It can perform the operations that are difficult (or) impossible in Finite Automata and Pushdown Automata.

The string called as palindrome if it is same in both forward and backward direction. For checking whether the given input string is the palindrome (or) not we need to check the first leftmost and right most characters. If both are same, then we must check second leftmost and rightmost characters. This step implemented for $n/2$ times. Where n stands for string length. Ex. For the string "racecar" the string length is seven. $7/2=3.5$ then removing the fractional part we will get the value as 3. The first leftmost character r checked with first rightmost character r. Both are same. Then second leftmost character a checked with the first rightmost character r. Both

*Author for correspondence

are same. Finally, third leftmost character c checked with first rightmost character c . Both are same. The value three reached. The result from step 1 to step 3 is true. Hence, the given string is the palindrome. If any case the result is false then the given string is not a palindrome.

1.1 Finite Automaton

The recognizer that accepts or rejects the input string called as a Finite Automaton (FA). The construction of Finite Automata based on the condition¹⁻³.

This FA is a quintuple. If FA represented as M then $M = (Q, \Sigma, \delta, q_0, F)$.

- Collection of states (Q).
- A finite set of input symbols called the alphabet (Σ).
- A transition function ($\delta : Q \times \Sigma \rightarrow Q$).
- A starting state ($q_0 \in Q$).
- A set of accepting state(s) ($F \subseteq Q$).

1.2 Turing Machine

The Turing Machine defined as a hypothetical device used to represent a computing machine⁴. It helps us to know the limitation of mechanical computation. It has seven tuples. Hence called as septuplet. It consists of

- A tape.
- A head.
- A state register.
- A finite table.

The head can move in both directions. This supports, the operations those are not possible in Finite Automata and Pushdown Automata.

Table 1. Replacement logic in the Turing Machine that accepts the palindrome

S. No.	First Character	Replaced Character	Last Character	Replaced Character
1	a	Blank	a	Blank
2	a	Blank	b	No replacement. Reach the halting state for rejection.
3	b	Blank	a	No replacement. Reach the halting state for rejection.
4	b	Blank	b	Blank

John C. Martin⁵ constructed a Turing Machine to accept the string that is palindrome⁵. The Turing Machine accepted both the odd length palindrome and even length palindrome. He used the two characters for forming the string. In two input characters, we need to check $n \times n$ combinations. Where n represents a total number of input characters. Therefore he used $2 \times 2 = 4$ combinations. Those are as shown in Table 1.

2. Construction of Finite Automata

In this work totally three input characters are used. Those are 'u' 'm' 'a'. The maximum string length restricted to five. The possible combinations of strings given in Table 2.

Table 2. Possible combination of string using three input characters up to string length five

S. No.	String Length	Possible Combination	Example
1	1	$3^1=3$	"u", "m", "a"
2	2	$3^2=9$	"uu", "um", "ua" ...
3	3	$3^3=27$	"uuu", "uum", "uua" ...
4	4	$3^4=81$	"uuuu", "uuum", "uuua" ...
5	5	$3^5=243$	"uuuuu", "uuuum", "uuuua" ...

The possible combinations of palindrome given in Table 3.

Table 3. Possible combination of palindrome using three input characters up to string length five

S. No.	String Length	Possible Combination	Example
1	1	$3^1=3$	"u", "m", "a"
2	2	$3^1=3$	"uu", "mm", "aa"
3	3	$3^2=9$	"uuu", "umu", "uau" ...
4	4	$3^2=9$	"uuuu", "ummu", "uaau" ...
5	5	$3^3=27$	"uuuuu", "uumuu", "uuauu" ...

3. Palindrome Derivation

The Finite Automata, which accepts palindrome for three input characters and string length, exactly five is shown

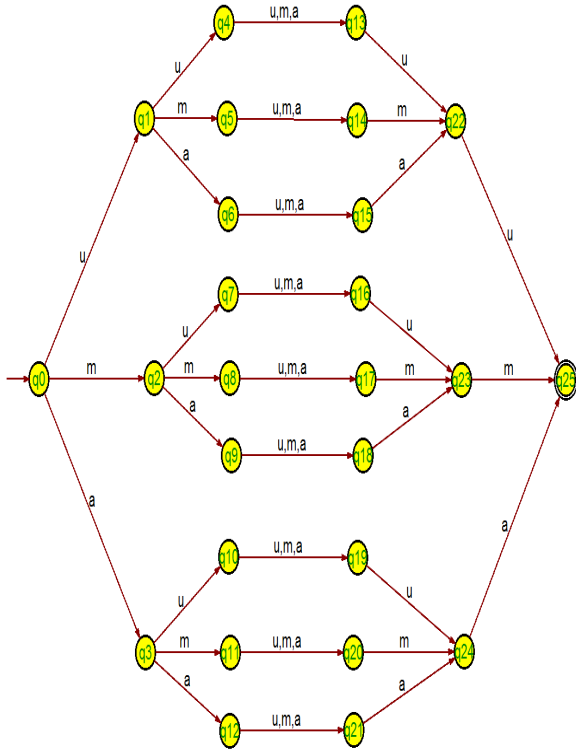


Figure 1. Transition Diagram - Finite Automata for accepting the string of length five exactly which is also palindrome using input characters 'u', 'm', 'a'.

in Figure 1. It accepts 27 possible palindromes out of 243 possible strings. It is possible to construct a Finite Automata that accepts all possible palindrome ranging from string length one to string length five. For that we need totally $3^0+3^1+3^2+3^3+3^4+3^5 = 1+3+9+27+81+243=364$ states as shown in Table 4.

Table 4. Collection of state for getting the string with length one to five

States	Input Characters		
	u	m	a
$\rightarrow q_0$	q ₁	q ₂	q ₃
*q ₁	q ₄	q ₅	q ₆
*q ₂	q ₇	q ₈	q ₉
*q ₃	q ₁₀	q ₁₁	q ₁₂
*q ₄	q ₁₃	q ₁₄	q ₁₅
q ₅	q ₁₆	q ₁₇	q ₁₈
q ₆	q ₁₉	q ₂₀	q ₂₁
q ₇	q ₂₂	q ₂₃	q ₂₄

*q ₈	q ₂₅	q ₂₆	q ₂₇
q ₉	q ₂₈	q ₂₉	q ₃₀
q ₁₀	q ₃₁	q ₃₂	q ₃₃
q ₁₁	q ₃₄	q ₃₅	q ₃₆
*q ₁₂	q ₃₇	q ₃₈	q ₃₉
*q ₁₃	q ₄₀	q ₄₁	q ₄₂
q ₁₄	q ₄₃	q ₄₄	q ₄₅
q ₁₅	q ₄₆	q ₄₇	q ₄₈
*q ₁₆	q ₄₉	q ₅₀	q ₅₁
q ₁₇	q ₅₂	q ₅₃	q ₅₄
q ₁₈	q ₅₅	q ₅₆	q ₅₇
*q ₁₉	q ₅₈	q ₅₉	q ₆₀
q ₂₀	q ₆₁	q ₆₂	q ₆₃
q ₂₁	q ₆₄	q ₆₅	q ₆₆
q ₂₂	q ₆₇	q ₆₈	q ₆₉
*q ₂₃	q ₇₀	q ₇₁	q ₇₂
q ₂₄	q ₇₃	q ₇₄	q ₇₅
q ₂₅	q ₇₆	q ₇₇	q ₇₈
*q ₂₆	q ₇₉	q ₈₀	q ₈₁
q ₂₇	q ₈₂	q ₈₃	q ₈₄
q ₂₈	q ₈₅	q ₈₆	q ₈₇
*q ₂₉	q ₈₈	q ₈₉	q ₉₀
q ₃₀	q ₉₁	q ₉₂	q ₉₃
q ₃₁	q ₉₄	q ₉₅	q ₉₆
q ₃₂	q ₉₇	q ₉₈	q ₉₉
*q ₃₃	q ₁₀₀	q ₁₀₁	q ₁₀₂
q ₃₄	q ₁₀₃	q ₁₀₄	q ₁₀₅
q ₃₅	q ₁₀₆	q ₁₀₇	q ₁₀₈
*q ₃₆	q ₁₀₉	q ₁₁₀	q ₁₁₁
q ₃₇	q ₁₁₂	q ₁₁₃	q ₁₁₄
q ₃₈	q ₁₁₅	q ₁₁₆	q ₁₁₇
*q ₃₉	q ₁₁₈	q ₁₁₉	q ₁₂₀
*q ₄₀	q ₁₂₁	q ₁₂₂	q ₁₂₃
q ₄₁	q ₁₂₄	q ₁₂₅	q ₁₂₆
q ₄₂	q ₁₂₇	q ₁₂₈	q ₁₂₉
q ₄₃	q ₁₃₀	q ₁₃₁	q ₁₃₂
q ₄₄	q ₁₃₃	q ₁₃₄	q ₁₃₅
q ₄₅	q ₁₃₆	q ₁₃₇	q ₁₃₈

Q46	Q139	Q140	Q141
Q47	Q142	Q143	Q144
Q48	Q145	Q146	Q147
Q49	Q148	Q149	Q150
Q50	Q151	Q152	Q153
Q51	Q154	Q155	Q156
*Q52	Q157	Q158	Q159
Q53	Q160	Q161	Q162
Q54	Q163	Q164	Q165
Q55	Q166	Q167	Q168
Q56	Q169	Q170	Q171
Q57	Q172	Q173	Q174
Q58	Q175	Q176	Q177
Q59	Q178	Q179	Q180
Q60	Q181	Q182	Q183
Q61	Q184	Q185	Q186
Q62	Q187	Q188	Q189
Q63	Q190	Q191	Q192
*Q64	Q193	Q194	Q195
Q65	Q196	Q197	Q198
Q66	Q199	Q200	Q201
Q67	Q202	Q203	Q204
*Q68	Q205	Q206	Q207
Q69	Q208	Q209	Q210
Q70	Q211	Q212	Q213
Q71	Q214	Q215	Q216
Q72	Q217	Q218	Q219
Q73	Q220	Q221	Q222
Q74	Q223	Q224	Q225
Q75	Q226	Q227	Q228
Q76	Q229	Q230	Q231
Q77	Q232	Q233	Q234
Q78	Q235	Q236	Q237
Q79	Q238	Q239	Q240
*Q80	Q241	Q242	Q243
Q81	Q244	Q245	Q246
Q82	Q247	Q248	Q249
Q83	Q250	Q251	Q252
Q84	Q253	Q254	Q255

Q85	Q256	Q257	Q258
Q86	Q259	Q260	Q261
Q87	Q262	Q263	Q264
Q88	Q265	Q266	Q267
Q89	Q268	Q269	Q270
Q90	Q271	Q272	Q273
Q91	Q274	Q275	Q276
*Q92	Q277	Q278	Q279
Q93	Q280	Q281	Q282
Q94	Q283	Q284	Q285
Q95	Q286	Q287	Q288
*Q96	Q289	Q290	Q291
Q97	Q292	Q293	Q294
Q98	Q295	Q296	Q297
Q99	Q298	Q299	Q300
Q100	Q301	Q302	Q303
Q101	Q304	Q305	Q306
Q102	Q307	Q308	Q309
Q103	Q310	Q311	Q312
Q104	Q313	Q314	Q315
Q105	Q316	Q317	Q318
Q106	Q319	Q320	Q321
Q107	Q322	Q323	Q324
*Q108	Q325	Q326	Q327
Q109	Q328	Q329	Q330
Q110	Q331	Q332	Q333
Q111	Q334	Q335	Q336
Q112	Q337	Q338	Q339
Q113	Q340	Q341	Q342
Q114	Q343	Q344	Q345
Q115	Q346	Q347	Q348
Q116	Q349	Q350	Q351
Q117	Q352	Q353	Q354
Q118	Q355	Q356	Q357
Q119	Q358	Q359	Q360
*Q120	Q361	Q362	Q363
*Q121	NIL	NIL	NIL
Q122	NIL	NIL	NIL
Q123	NIL	NIL	NIL
Q124	NIL	NIL	NIL
Q125	NIL	NIL	NIL
Q126	NIL	NIL	NIL
Q127	NIL	NIL	NIL

q ₁₂₈	NIL	NIL	NIL
q ₁₂₉	NIL	NIL	NIL
*q ₁₃₀	NIL	NIL	NIL
q ₁₃₁	NIL	NIL	NIL
q ₁₃₂	NIL	NIL	NIL
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*q ₁₃₉	NIL	NIL	NIL
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q ₂₇₀	NIL	NIL	NIL
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*q ₂₇₂	NIL	NIL	NIL
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*q ₂₈₁	NIL	NIL	NIL
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*q ₂₈₅	NIL	NIL	NIL
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q ₂₉₃	NIL	NIL	NIL
*q ₂₉₄	NIL	NIL	NIL
q ₂₉₅	NIL	NIL	NIL
q ₂₉₆	NIL	NIL	NIL
q ₂₉₇	NIL	NIL	NIL
q ₂₉₈	NIL	NIL	NIL
q ₂₉₉	NIL	NIL	NIL

q ₃₀₀	NIL	NIL	NIL
q ₃₀₁	NIL	NIL	NIL
q ₃₀₂	NIL	NIL	NIL
*q ₃₀₃	NIL	NIL	NIL
q ₃₀₄	NIL	NIL	NIL
q ₃₀₅	NIL	NIL	NIL
q ₃₀₆	NIL	NIL	NIL
q ₃₀₇	NIL	NIL	NIL
q ₃₀₈	NIL	NIL	NIL
q ₃₀₉	NIL	NIL	NIL
q ₃₁₀	NIL	NIL	NIL
q ₃₁₁	NIL	NIL	NIL
q ₃₁₂	NIL	NIL	NIL
q ₃₁₃	NIL	NIL	NIL
q ₃₁₄	NIL	NIL	NIL
*q ₃₁₅	NIL	NIL	NIL
q ₃₁₆	NIL	NIL	NIL
q ₃₁₇	NIL	NIL	NIL
q ₃₁₈	NIL	NIL	NIL
q ₃₁₉	NIL	NIL	NIL
q ₃₂₀	NIL	NIL	NIL
q ₃₂₁	NIL	NIL	NIL
q ₃₂₂	NIL	NIL	NIL
q ₃₂₃	NIL	NIL	NIL
*q ₃₂₄	NIL	NIL	NIL
q ₃₂₅	NIL	NIL	NIL
q ₃₂₆	NIL	NIL	NIL
q ₃₂₇	NIL	NIL	NIL
q ₃₂₈	NIL	NIL	NIL
q ₃₂₉	NIL	NIL	NIL
q ₃₃₀	NIL	NIL	NIL
q ₃₃₁	NIL	NIL	NIL
q ₃₃₂	NIL	NIL	NIL
*q ₃₃₃	NIL	NIL	NIL
q ₃₃₄	NIL	NIL	NIL
q ₃₃₅	NIL	NIL	NIL
q ₃₃₆	NIL	NIL	NIL
q ₃₃₇	NIL	NIL	NIL
q ₃₃₈	NIL	NIL	NIL
q ₃₃₉	NIL	NIL	NIL
q ₃₄₀	NIL	NIL	NIL
q ₃₄₁	NIL	NIL	NIL
q ₃₄₂	NIL	NIL	NIL

q ₃₄₃	NIL	NIL	NIL
q ₃₄₄	NIL	NIL	NIL
*q ₃₄₅	NIL	NIL	NIL
q ₃₄₆	NIL	NIL	NIL
q ₃₄₇	NIL	NIL	NIL
q ₃₄₈	NIL	NIL	NIL
q ₃₄₉	NIL	NIL	NIL
q ₃₅₀	NIL	NIL	NIL
q ₃₅₁	NIL	NIL	NIL
q ₃₅₂	NIL	NIL	NIL
q ₃₅₃	NIL	NIL	NIL
*q ₃₅₄	NIL	NIL	NIL
q ₃₅₅	NIL	NIL	NIL
q ₃₅₆	NIL	NIL	NIL
q ₃₅₇	NIL	NIL	NIL
q ₃₅₈	NIL	NIL	NIL
q ₃₅₉	NIL	NIL	NIL
q ₃₆₀	NIL	NIL	NIL
q ₃₆₁	NIL	NIL	NIL
q ₃₆₂	NIL	NIL	NIL
*q ₃₆₃	NIL	NIL	NIL

The Finite Automata, which accepts palindrome using three input characters and maximum string length, has 51 final states as shown in Table 5.

Table 5. Final States with accepted string from string length one to five

S. No.	String Length	Final State	Accepted String
1	1	q ₁	“u”
2	1	q ₂	“m”
3	1	q ₃	“a”
4	2	q ₄	“uu”
5	2	q ₈	“mm”
6	2	q ₁₂	“aa”
7	3	q ₁₃	“uuu”
8	3	q ₁₆	“umu”
9	3	q ₁₉	“uau”
10	3	q ₂₃	“mum”
11	3	q ₂₆	“mmm”
12	3	q ₂₉	“mam”
13	3	q ₃₃	“aua”

14	3	q ₃₆	"ama"
15	3	q ₃₉	"aaa"
16	4	q ₄₀	"uuuu"
17	4	q ₅₂	"ummu"
18	4	q ₆₄	"uaau"
19	4	q ₆₈	"muum"
20	4	q ₈₀	"mmmm"
21	4	q ₉₂	"maam"
22	4	q ₉₆	"auua"
23	4	q ₁₀₈	"amma"
24	4	q ₁₂₀	"aaaa"
25	5	q ₁₂₁	"uuuuu"
26	5	q ₁₃₀	"uumuu"
27	5	q ₁₃₉	"uuauu"
28	5	q ₁₅₁	"umumu"
29	5	q ₁₆₀	"ummmu"
30	5	q ₁₆₉	"umamu"
31	5	q ₁₈₁	"uauau"
32	5	q ₁₉₀	"uamau"
33	5	q ₁₉₉	"uaauu"
34	5	q ₂₀₃	"muuum"
35	5	q ₂₁₂	"mumum"
36	5	q ₂₂₁	"muaum"
37	5	q ₂₃₃	"mmummm"
38	5	q ₂₄₂	"mmmmmm"
39	5	q ₂₅₁	"mmamm"
40	5	q ₂₆₃	"mauam"
41	5	q ₂₇₂	"mamam"
42	5	q ₂₈₁	"maaam"
43	5	q ₂₈₅	"auuua"
44	5	q ₂₉₄	"aumua"
45	5	q ₃₀₃	"auaua"
46	5	q ₃₁₅	"amuma"
47	5	q ₃₂₄	"amma"
48	5	q ₃₃₃	"amama"
49	5	q ₃₄₅	"aauaa"
50	5	q ₃₅₄	"aamaa"
51	5	q ₃₆₃	"aaaaa"

4. Conclusion

The Turing Machine offers a fast construction for accepting a palindrome. Comparing with Turing Machine the possible combination of the path is equal for the Finite Automata. The string length constraint not considered in the Turing Machine. In case of Finite Automata string length plays a vital role in designing an abstract machine. The designing of Finite Automata for accepting the palindrome is an effective resource management technique. Because without Turing Machine it is possible to construct an abstract machine for accepting the palindrome.

5. Future Work

This work further may be implemented for the available palindrome in the dictionary. The number of the palindrome and its length is already available. So it is possible to construct the Finite Automata for the palindrome.

6. References

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