

A Multi-Objective Approach for Improving Technical Factors of Distribution Networks Considering Uncertainties in Loads and Wind Turbines

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Abstract

Objectives: Objectives of this paper are to achieve decreasing power losses, maintaining permissible voltage profiles in distribution networks and also considering the uncertainties of network Components like loads and wind turbines. **Methods/Statistical Analysis:** A new method is proposed for Distribution Feeder Reconfiguration (DFR) and capacitor placement considering Wind Turbine (WT) based on an improved reconfiguration technique. The employed DFR method is based on a single loop reconfiguration method which selects the optimal branch in each loop to achieve maximum loss reduction. Moreover, sequence of loops selection is optimized by using an optimization algorithm. **Findings:** A joint optimization algorithm has been proposed for combination of the capacitor placement and the improved network reconfiguration. This is due to the inherent coupling relationship between these methods, and therefore, simultaneous implementation of them is more effective than considering them separately. For more practical application of the proposed method, stochastic nature of loads and wind turbine generators of the network have been considered. Teaching-Learning Based Optimization (TLBO) algorithm has been employed for the proposed joint optimization problem and its results have been compared to the PSO and GA. The objective function has been proposed for minimizing the total cost due to capacitor placement and energy losses during 2 years with considering the constraints of bus voltages and the current carrying capacity of conductors. The obtained results confirmed the effectiveness of the proposed method. **Application/Improvements:** Simultaneous implementation of capacitor placement and reconfiguration method, considering stochastic nature of network and also employing TLBO algorithm for the proposed optimization problem.

Keywords: Load and Technical Improvement, Distribution Network, Uncertainty, Wind Turbine

1. Introduction

Nowadays the concern about energy shortage, economic features of fuel saving and also, environmental pollution problems increase interests in using of renewable energy resources¹⁻³. Wind turbine is one

of the major ways to generate electrical energy from renewable resources which converts the flowing wind energy into electrical energy. Distribution Feeder Reconfiguration (DFR) problem is one of the most important problems in distribution systems which could be affected by WTs^{4,5}.

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Electrical power losses exist in different parts of power system from generation to the end users; however, contribution of distribution systems in power losses is greater than other parts. Two important approaches to reduce power losses in distribution systems are DFR and capacitor placement. In the DFR, optimal network topologies could be obtained using tie and sectionalizing switches which their mood assign the configuration of distribution network, so that, the radial structure of the network is preserved. Also, capacitor placement in distribution networks maximizes power loss reduction. Indeed, parallel capacitors not only reduce losses, but also enhance the voltage curve, power factor, and voltage stability of the system. The size and location of the capacitors determine the level of compensation. In order to access optimal configuration of distribution network and capacitor installation, numerous efforts have been carried out recently⁶⁻¹¹. In¹² a joint optimization process combining Minimum Nodal Voltage method (MNV) and Genetic Algorithms (GA) is performed to rearrange the network configuration and solve capacitor placement problem, respectively. The effectiveness of simultaneously applying these strategies in reducing power dissipation is more than that of each method alone¹². The research done in¹³ presents an efficient algorithm for optimization of radial distribution systems dealt with by a joint strategy using a network reconfiguration and capacitor allocation method. This modified genetic algorithm-based approach remarkably saved the purchasing cost of new capacitor banks, decreased the computational burden and improved the quality of the configurations. In¹⁴ to optimize the capacitor placement, an Improved Adaptive Genetic Algorithm (IAGA) is employed. Meanwhile, for each genetic chromosome, a simplified branch exchange technique is developed to reach the optimal network topology. In¹⁵, the state of capacitors and branch exchange in each loop was effectively achieved employing the Ant Colony Search Algorithm (ACSA). However, the branch which must be opened in each loop is not still the optimal one in primary iterations. Moreover, in¹⁴, the branch to be opened at each loop was precisely analyzed using a simple method in all iterations of the GA, and it is unnecessary to calculate the power loss reductions of all possible branch exchanges in determining an optimal branch exchange.

The DFR method used in this paper is based on the single loop reconfiguration method illustrated in¹⁴. In

this method, the branch to be opened is formulated by mathematical equations in single loop networks. The single loop reconfiguration method is carried out on the networks loops respectively, while the sequence of loops selection is highly effective to achieve optimal network configuration due to the maximum power loss reduction. The significant innovation of our DFR method is to optimize the sequence of loops for rearrangement by single loop reconfiguration method. In subsequent parts of the paper, we have proven the effect of loops selection sequence on power loss reduction by providing examples in the under studying distribution network. DFR and capacitor placement which affect the optimal configuration and the power losses, have not been simultaneously incorporated in distribution networks which has wind turbine generators, up to now. It's obvious that by simultaneous implementation of DFR and capacitor placement, the most optimal network configuration will be obtained. Consequently, in iterations of the proposed optimization algorithm, not only capacitor modes are selected, but the loops selection sequence also is determined. Finally, due to access to the optimal distribution network configuration for maximum loss reduction, a joint optimization algorithm is proposed for combining the reconfiguration method and capacitor placement in distribution network with WT units. In order to select the best sequence for loops and optimize the location and capacitors' values, a strong optimization algorithm is needed. In our work, Teaching-Learning Based Optimization (TLBO) algorithm is used, which is more efficient and recently developed^{16,17}. Simulation results confirm the validity of this optimization algorithm.

In addition to above mentioned, the DFR problem could be affected by WT and loads uncertainty. In this paper, for modeling variation generation of WTs and loads, we have used a scenario-based approach for modeling the stochastic nature of WT and loads demand. To consider stochastic nature of wind speed and loads magnitudes, in this paper they are modeled by normal Probability Density Function (PDF). Consequently, a network scenario is obtained by roulette wheel mechanism which is applied to each load and WT as for their PDF. As can be illustrated in section 3, the stochastic trend in uncertainty of these parameters is simulated by creating scenarios which can be solved by deterministic methods. In order to experimentally verify the numerically-obtained

results, the simulation data are simultaneously tested on a region of realistic distribution network in Karaj city in Iran.

2. Proposed Reconfiguration Method

In initial configuration of distribution networks there are some lines which are normally open due to keeping the radial topology of the network. These lines are switched off by a switch (connector switch). In order to improve the networks reliability, one of these lines enters into the circuit and prevents some loads disruption only when one of the lines switched off in the network.

As already mentioned, when these lines are connected, a loop is formed in the network. In this loop, by opening the circuit breakers of both sides of a line, network takes radial structure. In this part a method is introduced to determine the lines which should be disrupted in order to have the minimum power losses according to its radial structure.

2.1 Reconfiguration Method for Single Loop

In¹⁴ an efficient method is proposed to determine the optimal line which should leave the circuit in the single loop. For this, in Figure 1 it is assumed that branches $\{i, \dots, n\}$ named to be the U set and branches $\{j, \dots, m\}$ named to be the D set. In addition, r_K is resistance of the branch associated with the switch K . A power equals to $P_K + Q_K$ be transmitted between two sets when the switch K is turned off and a separator switch is turned on. It should be mentioned that the transferred power is a continuous variable which transfers from $U - D$.

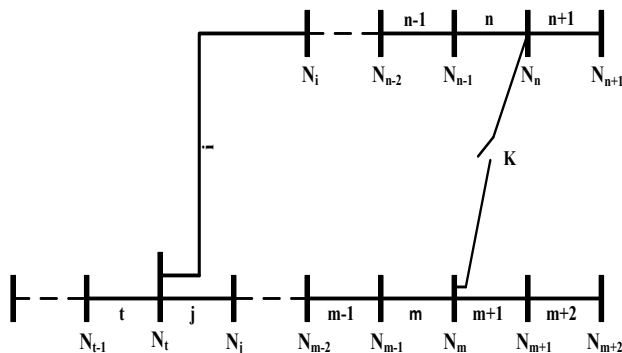


Figure 1. A distribution network with single loop.

After mentioned transformation the power loss reduction is obtained by Equation (1).

$$P_{loss}^{reduction} = P_{loss}^{before} - P_{loss}^{after} = 2 \sum_{i \in U} [P_i P_K + Q_i Q_K] r_i - 2 \sum_{i \in D} [P_i P_K + Q_i Q_K] r_i - (P_K^2 + Q_K^2) r_K \quad (1)$$

where $P_{loss}^{reduction}$ is power loss reduction, P_{loss}^{before} is power loss before reconfiguration, and P_{loss}^{after} is power loss after running reconfiguration method. P_i and Q_i are active and reactive power which are transmitted by lines.

In order to find the optimal power transmitted $P_K + Q_K$ that maximizes the power loss reduction, $P_{loss}^{reduction}$ partial derivation related to P_K and Q_K must be equal to zero using Equation (2).

$$\begin{cases} \frac{\partial P_{loss}^{reduction}}{\partial P_K} = 0 \\ \frac{\partial P_{loss}^{reduction}}{\partial Q_K} = 0 \end{cases} \quad (2)$$

Considering the Equation (2), the optimal power to transmit between two sets is found according to Equation (3).

$$\begin{cases} P_K = \frac{\sum_{i \in U} P_i r_i - \sum_{i \in D} P_i r_i}{\sum_{i \in D \cup U} r_i + r_K} \\ Q_K = \frac{\sum_{i \in U} Q_i r_i - \sum_{i \in D} Q_i r_i}{\sum_{i \in D \cup U} r_i + r_K} \end{cases} \quad (3)$$

To specify the line with optimal power transmission, following constraints regarding transferred power symbol and quantity are defined.

If $P_K < \frac{P_n}{2}$ or $P_K < \frac{P_m}{2}$, real power loss in the loop already was minimum and the switch K must be remain open.

If P_K has a positive value, the optimal power is transferred from $U - D$. In set U the branch that has the closest value to P_K must be switched off.

Similarly, If P_K has a negative value, the optimal power is transferred from D to U . In this case, the branch in the set D that has the closest value to P_K must be switched off.

2.2 Reconfiguration Method in Looped Distribution Networks

Like one loop method which was presented in the previous section, connector switches are respectively chosen and

the associated loop with each connector switch is distinguished and the line which should be opened is detected and opened. Such procedure is similarly done for the other connectors. The point which should be mentioned is that this method does not give the optimal lines to be opened, because selection order of connector switches is influenced in the lines which should be opened and consequently affects network configuration and its power loss.

At first, it is supposed that all the connector lines are open and then one connector is selected as the first connector and as shown in Figure 1, D and U sets are determined. In the second step, a line that should be left from U and D sets is identified. This scheme is also done for the other connector lines. In¹⁴, connector switches are selected without any priority order, whereas, but connector lines selection order influences on some lines that must be departed from circuit and consequently affects network losses.

3. Generating Stochastic Model for Network Loads and Wind Turbines

3.1 Generating Network Scenarios

In this paper, to achieve a high accuracy in prediction of WTs and loads active power, their uncertainty is considered based on the forecast error of WTs and loads active power. Accordingly, a typical PDF has been employed to considering the forecast error of WTs and loads. The used continuous distribution function of forecast error of WTs and loads active power along with their discretization is shown in Figure 2. As shown in Figure 2, some intervals are on the zero mean and each of intervals is one forecast error of WTs or loads active power standard deviation, as presented in¹⁸. Finally, a roulette wheel mechanism is implemented to generate scenarios for a specified time¹⁹. The generated scenarios are selected on the basis of different forecast levels of WTs and loads and their obtained probabilities from their related PDF.

To this end, at first, the probabilities of different forecast levels of WTs and loads active power are normalized such that their summation becomes equal to one. Therefore, using roulette wheel mechanism, their scenario is formed. In this regards, as shown in Figure 3, the interval of $[0,1]$ is allocated to the normalized probabilities. After that, random numbers are

generated between 0 and 1. Each generated number is situated in the normalized probability range of forecast level in the roulette wheel (Figure 3). The selected interval is associated with a binary digit equal to one, and others become zero. After obtaining forecast level for all of the loads and wind speeds, a scenario of the network is produced.

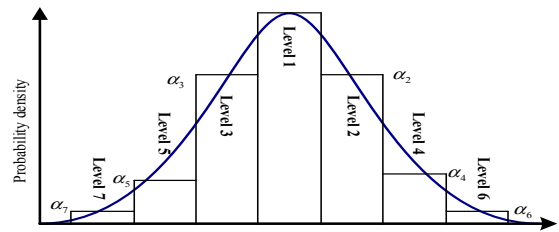


Figure 2. Discretization of PDF of load and wind speed error.

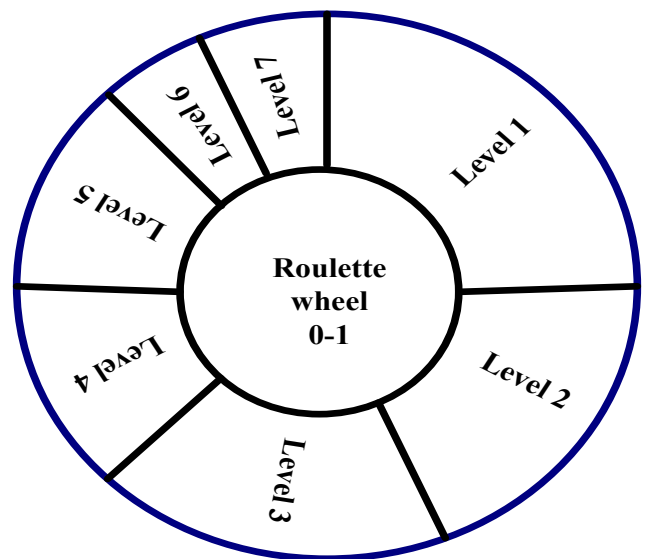


Figure 3. Roulette wheel selection.

A scenario is a vector that identifies the charge interval of all loads and WTs. Intended number of scenarios is produced by scenario generating scheme. Finally, the probability of all scenarios is calculated using Equation (4).

$$P_{Scenario} = \frac{\prod_{j=1}^{N_{WT}} \sum_{i=1}^7 w_{n,i,j}^{WT} \cdot \alpha_{n,i,j} \cdot \prod_{m=1}^{N_{load}} \sum_{r=1}^7 w_{n,r,m}^{load} \cdot \alpha_{n,r,m}}{\sum_{k=1}^{N_{scen}} \left(\prod_{j=1}^{N_{WT}} \sum_{i=1}^7 w_{n,i,j}^{WT} \cdot \alpha_{n,i,j} \cdot \prod_{m=1}^{N_{load}} \sum_{r=1}^7 w_{n,r,m}^{load} \cdot \alpha_{n,r,m} \right)} \quad (4)$$

where N_{WT} is the number of WTs, N_{load} is the number of loads, $w_{n,i,j}^{WT}$ is binary parameter indicating whether the i -th wind interval of j -th WT is selected in the n th scenario, and N_{scen} is the number of scenarios.

3.2 Reduction of the Scenarios

A scenario reduction mechanism is employed to reduce the number of scenarios. On this basis, a good approximation of the system uncertain behavior is preserved²⁰. For scenario reduction, the proposed mechanism has following steps:

Step 1: Construct the Kantorovich Distance (KD) matrix²¹. KD of each pair scenario is calculated by Equation (5).

$$KD(Scen^i, Scen^j) = \left(\sum_{s=1}^{N_L + N_{WT}} P_s^i + P_s^j \right)^{0.5} \quad (5)$$

Step 2: Determine the other nearest scenario to each scenario by calculated KD in step 1, and mark that in the KD matrix ($\min\{KD(Scen^i, Scen^j)\}$).

Step 3: Compute the following term in Equation (6) for each pair of scenarios in the second step.

$$kp^{i,j} = \min\{KD(Scen^i, Scen^j)\} \times P[Scen^i] \quad (6)$$

Compare the $kp^{i,j}$ for all scenario pairs in the KD matrix and locate, which pair has the minimum value. From this two scenarios, which one should be eliminated is chosen based on:

- Relative closeness to other scenarios.
- Small probability of occurrence.

Step 4: After eliminating one scenario, its probability is added to the probability of the closest scenario and the new KD matrix is constructed.

Step 5: Go to step 2 and eliminate a scenario in iteration until the desired number of scenarios is obtained. In this paper, 10 representative scenarios at the end of iteration from the initial 1000 produced scenarios are considered.

4. Optimization Method

As mentioned, in a joint optimization problem, the purpose is to optimize several objectives simultaneously while some constraints should be met. In this paper,

the proposed method of reconfiguration is combined with the capacitor placement by a joint optimization algorithm. The simplified branch exchange algorithm is used to find the optimal network structure (by considering the specified sequence of loops selection) for each instance of optimization algorithm in the each iteration of capacitor optimization algorithm. The mentioned optimization algorithm is Teaching-Learning Based Optimization (TLBO) algorithm.

The TLBO algorithm is based on the effect of a teacher performance on the learner's marks in a class¹⁶. An advantageous teacher produces a better mean for learner's marks in exam. Learners also learn from interaction with each other, which also helps them to leave and makes their marks better. In TLBO, different design variables are considered as different course subjects who presented to learners and the learners' result is considered as the 'fitness'. The best solution which is obtained so far is called the 'teacher level' of TLBO algorithm. The step-wise procedure for implementation of TLBO is divided into two parts. The first part is 'teacher phase' and the other part is 'learner phase'. The 'teacher phase' means making progress in students' knowledge by learning from the teacher and the obtained progress in students' knowledge by interaction between themselves is occurred in 'Learner phase'^{16,17}. The flow chart of TLBO operation is shown in Figure 4.

The main computational procedure of the joint optimization can be stated using a flowchart as shown in Figure 5. DIGSILENT Programming Language (DPL) is used to calculate the objective function of the paper. TLBO algorithm which is used to optimize capacitor placement and sequence of loops selection has been implemented by the MATLAB software. The capacitors mode and sequence of loops selection are produced by TLBO algorithm in MATLAB software based on the value of objective function and are recorded in a text file. DIGSILENT reads it as input data and applies them to the network (perform capacitor placement and apply the sequence of loops selection to the network for reconfiguration). Then, load flow calculation is run and the constraints are checked and the value of the objective function is calculated. Again, value of the objective function is given to MATLAB as input data via a text file. This procedure will be repeated until the result is converged.

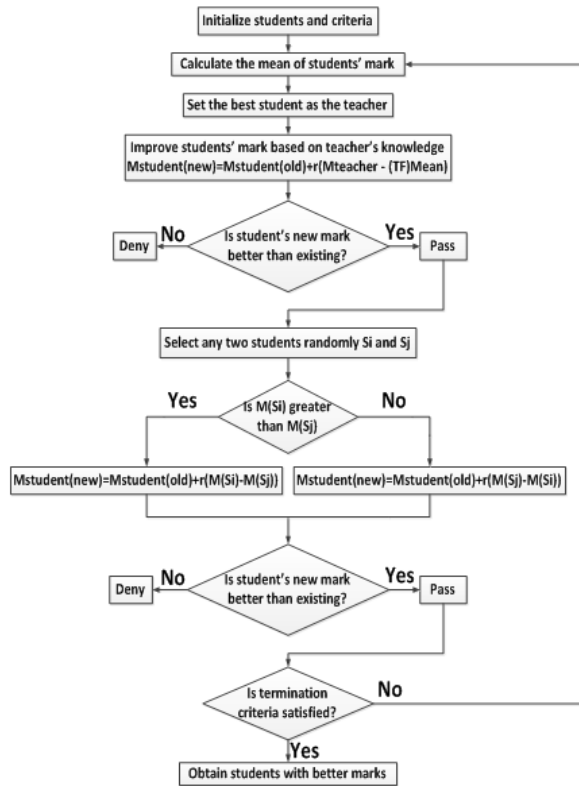


Figure 4. Flow chart of TLBO algorithm performance.

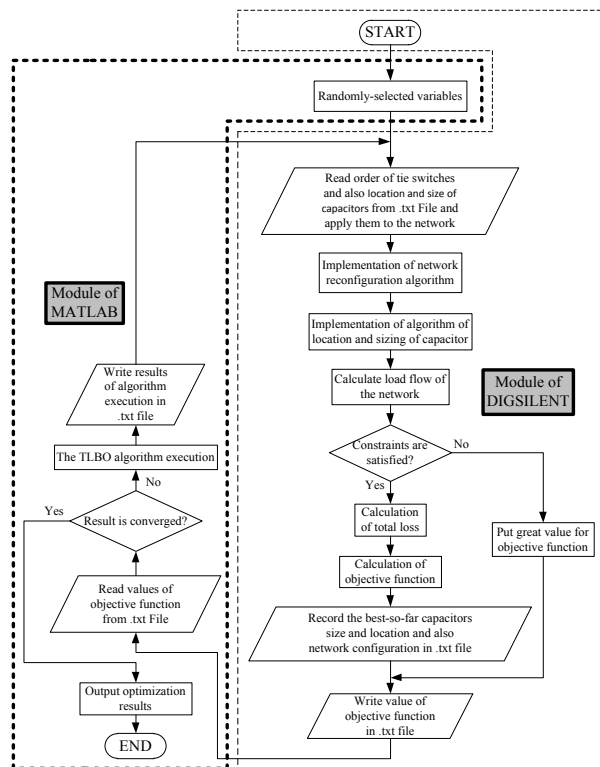


Figure 5. Flow chart of joint optimization algorithm.

5. Simulation Results

In this section, an 87-Bus radial distribution system with WTs is considered to evaluate the proposed optimization approach. This distribution network is a real life distribution network of the city of Karaj in Iran which is shown in Figure 6. This distribution network has 13 tie switches. Total consumption of network is 18.88 MW and 4.73 MVAR and active power loss of its' initial configuration is 504.094 kW.

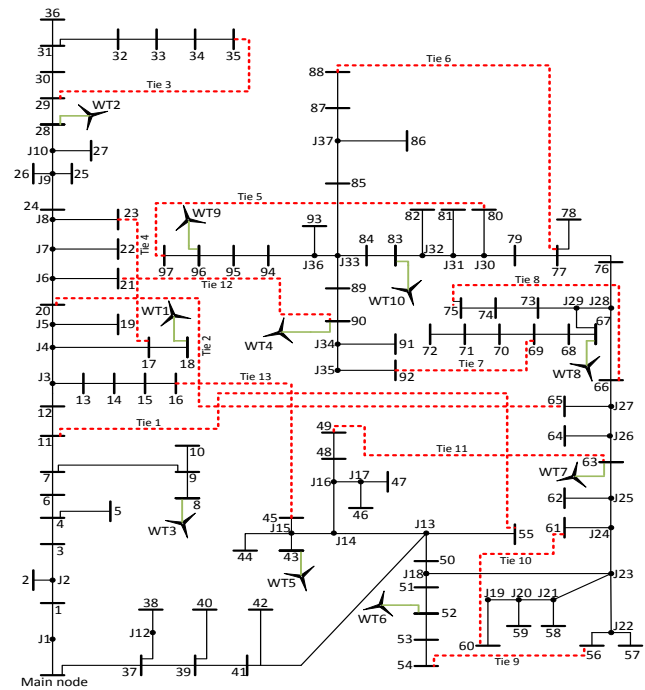


Figure 6. The study case distribution network.

The objective function of this paper is to minimize the total cost of network configuration which is formed by two portions: capacitor placement cost and energy losses cost. For this purpose, as we were sure that until the next year no changes will happen to the network, the network life is considered to be 2 years. The life time of capacitors which is used in this paper is supposed to be 20 years, so the cost of the installed capacitors is assumed to be 2/20 of the capacitors purchase cost.

The sizes of the capacitors used in this paper have discontinuous magnitudes and have selected of 19 kinds of capacitors produced by IRAN TRANSFO factory which is presented in Equation 1.

Mathematical definition of the objective function proposed in this paper is shown in Equation (7). To

Table 1. Information of capacitors used in this paper.

Order	Capacitor capacity (kVAr)	Purchase cost (\$)	Installation cost (\$)	Order	Capacitor capacity (kVAr)	Purchase cost (\$)	Installation cost (\$)
1	0	0	0	11	225	1508	139
2	50	459	43	12	250	1629	139
3	70	555	43	13	265	1925	155
4	100	693	70	14	275	1967	182
5	125	814	70	15	290	2263	198
6	150	1152	112	16	300	2088	182
7	170	1249	112	17	315	2384	198
8	175	1273	112	18	325	2201	209
9	195	1370	112	19	335	2480	198
10	200	1387	139				

optimize this objective function, we consider constraints that are, limits on bus voltages and also capacity of current carrying of conductors as given in Equation (8) and Equation (9).

$$F_{objective} = 2 \times 365 \times k_{cost}^{energy} \times E_{Loss}^{daily} + \sum (K_{cost}^{installation} + \frac{K_{cost}^{purchase}}{10}) \quad (7)$$

$$V_{min} \leq |V_i| \leq V_{max} \quad (8)$$

$$I_L \leq I_{max(L)} \quad (9)$$

where $k_{cost}^{installation}$ is cost of energy which is equal to 77.3\$/MWh, E_{Loss}^{daily} is daily energy losses, $K_{cost}^{installation}$ is installation cost of capacitors, $K_{cost}^{purchase}$ is purchase cost of capacitors, V_{min} and V_{max} are minimum and maximum

permissible bus voltages (equal to 0.95 and 1.05 p.u., respectively), and $I_{max(L)}$ is current carrying capacity of line L .

5.1 Stochastic Model for Loads and WTs

In the case study of Figure 6, we consider stochastic model for loads and wind turbines. For modeling network loads and WTs generation based on the method which has been presented in section 3. Firstly, we create 1000 scenarios, and then we reduce these 1000 scenarios to 10 scenarios by the proposed scenario reduction method. The aggregated scenario can be obtained by considering probability of these 10 scenarios. Results of applying this stochastic model for active power generation of each ten WTs are given in Table 2.

Table 2. Stochastic model for active power of WTs (kW).

	WT 1	WT 2	WT 3	WT 4	WT 5	WT 6	WT 7	WT 8	WT 9	WT 10
Scenario 1	286	300	321.3	300	306.67	292.673	314.16	299.83	306.67	279.32
Scenario 2	286	307	314.1	307	293	286	307	286.16	286.16	286
Scenario 3	286	307	292.6	293	313.5	299.347	307	293	293	279.32
Scenario 4	279.32	300	307	307	293	292.673	307	293	293	286
Scenario 5	279.32	300	307	307	299.83	286	307	293	279.32	265.98
Scenario 6	272.65	307	299.8	300	299.83	286	314.16	286.16	299.83	292.67
Scenario 7	292.67	300	314.1	307	293	279.327	307	279.32	293	299.34
Scenario 8	286	286	299.8	314	279.32	286	299.83	293	299.83	299.34
Scenario 9	286	314	299.8	300	299.83	272.653	314.16	306.67	293	279.32
Scenario 10	292.67	300	307	321	299.83	286	299.83	293	286.16	279.32

5.2 Effects of Different Loop Selection on Network Reconfiguration

In this section, we have illustrated the importance of loop selection sequence on distribution networks' loss reduction. To this end, we have implemented the best and the worst sequence of loop selection on deterministic and aggregated scenarios of networks. As demonstrated in Table 3, by selecting the best case for loops sequence, network power losses would be minimum state.

5.3 Optimization Algorithms Comparison

In this section, we have compared the results of TLBO algorithm with that of the PSO and GA algorithms. For this purpose, we have implemented these algorithms to the proposed distribution network in two load models: Aggregated and Deterministic scenarios. In comparison of these optimization algorithms, we have noticed

to the capacity of installed capacitors, their costs and also actual power losses magnitudes in Table 4. The branches that must be opened are brought in Table 5.

We can see from the Table 4 and 5 and also convergence curves of three algorithms in Figure 7 that TLBO algorithm has better performance compared with PSO and GA and it reaches to the best case of network configuration in less iteration than other algorithms.

Since in implementing of these scenarios to the assumed distribution network, we have applied constraint of Bus bars voltage magnitude in our simulations, so suitable configurations to the under studying distribution network is achieved. In Figure 8, the obtained profile voltage for 10 representative scenarios is shown. Also, the profile voltage of the deterministic and the aggregated scenarios is shown in Figure 9.

Table 3. Importance of sequence of loops selection.

Best case					Worst case						
Deterministic Scenario			Aggregated Scenario		Deterministic Scenario			Aggregated Scenario			
Network loss = 473.938 kW			Network loss = 485.098 kW		Network loss = 497.802 kW			Network loss = 507.563 kW			
Sequence of network loops selection	Branches that must be opened		Sequence of network loops selection	Branches that must be opened		Sequence of network loops selection	Branches that must be opened		Sequence of network loops selection	Branches that must be opened	
	from	to		from	to		from	to		from	to
Tie12	84	J33	Tie3	34	35	Tie9	J22	J23	Tie1	55	J13
Tie1	Tie1		Tie12	84	J33	Tie8	J28	J29	Tie10	Tie10	
Tie13	13	J3	Tie13	13	J3	Tie4	25	J9	Tie7	90	J34
Tie5	94	J36	Tie11	Tie11		Tie3	34	35	Tie6	85	J37
Tie9	J22	J23	Tie8	73	J29	Tie13	45	J15	Tie13	45	J15
Tie10	J19	J20	Tie1	Tie1		Tie10	Tie10		Tie5	94	J36
Tie6	Tie6		Tie4	25	J9	Tie7	92	J35	Tie12	J30	J31
Tie3	34	35	Tie10	J19	J20	Tie2	65	J27	Tie2	Tie2	
Tie8	73	J29	Tie6	87	J37	Tie5	94	J36	Tie4	25	J9
Tie7	J34	J35	Tie7	J34	J35	Tie12	84	J33	Tie3	34	35
Tie4	25	J9	Tie2	65	J27	Tie1	Tie1		Tie8	73	J29
Tie2	65	J27	Tie5	Tie5		Tie6	87	J37	Tie11	Tie11	
Tie11	Tie11		Tie9	J22	J23	Tie11	Tie11		Tie9	J22	J23

Table 4. Comparison of three algorithms.

Optimization algorithm	TLBO		PSO		GA	
	Aggregated scenario	Deterministic scenario	Aggregated scenario	Deterministic scenario	Aggregated scenario	Deterministic scenario
Installed cap. (MVA)	7.715	6.3	7.945	6.415	8.335	6.655
Cap. Cost (\$)	10637.7	8875	10930.9	9059.8	11415.5	9371
Actual power losses (kW)	485.098	473.938	485.34	473.9	486.258	474.035
Total cost	667603.8684	650727.3868	668224.6821	650860.4253	669952.6248	651354.6678

Table 5. Branches that should be open by three algorithms.

GA		PSO				TLBO					
Deterministic scenario		Aggregated scenario		Deterministic scenario		Aggregated scenario		Deterministic scenario		Aggregated scenario	
from	to	from	to	from	to	from	to	from	to	from	to
34	35	84	J33	34	35	34	35	85	J37	34	35
25	J9	25	J9	84	J33	Tie11		65	J27	84	J33
84	J33	85	J33	85	J33	94	J63	84	J33	13	J3
J22	J23	34	35	Tie1		84	J33	34	35	Tie11	
13	J3	J19	J20	Tie2		13	J3	73	J29	73	J29
90	J34	J22	J23	73	J29	25	J9	13	J3	Tie1	
96	97	Tie1		J34	J35	Tie1		Tie11		25	J9
	Tie11	J34	J35	J22	J23	73	J29	95	96	J19	J20
	Tie2	13	J3	13	J3	Tie6		Tie1		87	J37
73	J29	73	J29	J19	J20	Tie2		J19	J20	J34	J35
	Tie6	80	J30	Tie11		Tie7		J22	J23	65	J27
J19	J20	65	J27	25	J9	J19	J20	25	J9	Tie5	
	Tie1	Tie11		80	J30	J22	J23	J34	J35	J22	J23

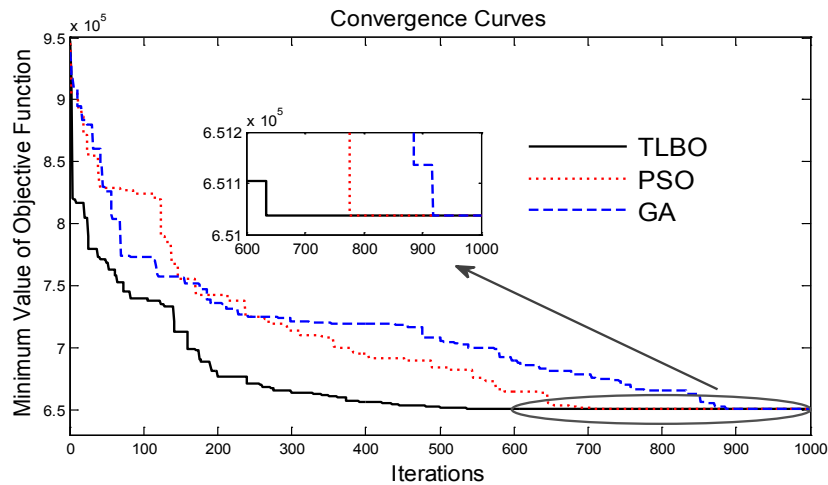


Figure 7. Convergence curves for the proposed three optimization algorithms.

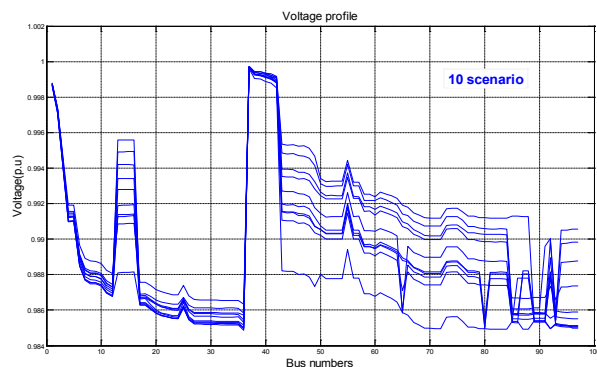


Figure 8. Voltage profile for 10 scenarios.

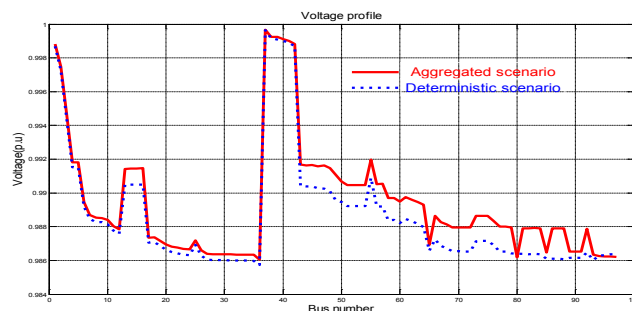


Figure 9. Voltage profile for aggregated and deterministic scenarios.

Table 6. Results of scenarios.

Best case						Worst case					
Deterministic Scenario			Aggregated Scenario			Deterministic Scenario			Aggregated Scenario		
Network loss = 473.938 kW						Network loss = 485.098 kW					
Sequence of network loops selection	Branches that must be opened		Sequence of network loops selection	Branches that must be opened		Sequence of network loops selection	Branches that must be opened		Sequence of network loops selection	Branches that must be opened	
	from	to		from	to		from	to		from	to
Tie12	84	J33	Tie3	34	35	Tie9	J22	J23	Tie1	55	J13
Tie1	Tie1		Tie12	84	J33	Tie8	J28	J29	Tie10	Tie10	
Tie13	13	J3	Tie13	13	J3	Tie4	25	J9	Tie7	90	J34
Tie5	94	J36	Tie11	Tie11		Tie3	34	35	Tie6	85	J37
Tie9	J22	J23	Tie8	73	J29	Tie13	45	J15	Tie13	45	J15
Tie10	J19	J20	Tie1	Tie1		Tie10	Tie10		Tie5	94	J36
Tie6	Tie6		Tie4	25	J9	Tie7	92	J35	Tie12	J30	J31
Tie3	34	35	Tie10	J19	J20	Tie2	65	J27	Tie2	Tie2	
Tie8	73	J29	Tie6	87	J37	Tie5	94	J36	Tie4	25	J9
Tie7	J34	J35	Tie7	J34	J35	Tie12	84	J33	Tie3	34	35
Tie4	25	J9	Tie2	65	J27	Tie1	Tie1		Tie8	73	J29
Tie2	65	J27	Tie5	Tie5		Tie6	87	J37	Tie11	Tie11	
Tie11	Tie11		Tie9	J22	J23	Tie11	Tie11		Tie9	J22	J23

Table 7. Capacitor placement for aggregated scenario.

Bus No.	kVAR	Bus No.	kVAR	Bus No.	kVAR	Bus No.	kVAR	Bus No.	kVAR	Bus No.	kVAR	Bus No.	kVAR
2	70	18	70	32	200	44	70	58	50	73	300	85	170
3	70	19	175	33	250	45	50	59	50	74	100	87	195
4	100	20	50	34	70	48	100	60	265	75	195	89	195
5	50	21	50	35	125	49	100	62	250	76	50	90	50
6	50	24	100	37	125	50	70	63	70	77	50	91	225
7	70	25	70	38	70	51	100	65	70	78	195	93	100
9	50	26	100	40	50	52	50	68	100	79	70	94	125
14	225	28	125	41	50	53	70	69	100	81	70	95	125
15	125	29	175	42	70	54	70	71	275	82	70		
17	70	31	150	43	150	57	70	72	170	84	175		

Table 8. Capacitor placement for deterministic scenario.

Bus No.	kVAr	Bus No.	kVAr	Bus No.	kVAr	Bus No.	kVAr	Bus No.	kVAr	Bus No.	kVAr	Bus No.	kVAr
1	50	16	70	25	265	39	50	59	175	74	225	89	100
3	70	17	175	27	170	40	50	61	195	76	100	90	175
4	70	18	50	28	50	46	175	64	50	77	70	91	250
7	70	19	50	30	70	47	70	65	50	78	170	93	70
9	50	20	70	31	50	49	70	67	195	79	70	96	150
10	100	21	125	32	70	51	70	69	150	81	100	97	50
11	175	22	70	35	175	53	125	71	70	82	195		
12	50	23	70	37	70	56	50	72	50	84	50		
15	50	24	250	38	125	57	150	73	50	85	70		

By comparing the obtained results in Tables 3, 6-8 and also Figure 8 and 9, it is obvious that there are difference between the results of deterministic scenario, ten representative scenarios and aggregated scenario. In addition, the probability of the deterministic scenario is about 4.4% (among 1000 produced scenarios). This means that the deterministic solution may happen with the low probability of 4.4%. Consequently, the deterministic scenario cannot be an acceptable solution by itself. On the other hand, using the obtained representative scenarios, all 10 scenarios contribute into determining the DNR results according to their probability values. The 10 representative scenarios totally capture about 10.6% of the uncertainty spectrum of the wind speed, which is about 2.5 times of the deterministic scenario. So, the DFR results of the stochastic framework are more realistic than the deterministic one. It should be noted that it can be more than 10.6%, considering more scenarios, but with the cost of higher computation burden. Based on the above expression, there is a trade-off between computation burden and model reality. In this case, the number of representative scenarios will be selected based on decision maker priority. Additionally, the most important advantage of scenario aggregation is that individual scenarios' problems become simple to interpret and with aggregation the representative scenarios the underlying problem structure is preserved.

6. Conclusion

In this paper, the network reconfiguration algorithm which was proposed in¹³ has been improved by optimization of the loops selection sequence. Moreover, a joint

optimization algorithm has been proposed for combination of the capacitor placement and the improved network reconfiguration. This is due to the inherent coupling relationship between these methods, and therefore, simultaneous implementation of them is more effective than considering them separately. For more practical application of the proposed method, stochastic nature of loads and wind turbine generators of network have been considered. TLBO algorithm has been employed for the proposed joint optimization problem and its results have been compared to the PSO and GA. The objective function has been proposed for minimizing the total cost due to capacitor placement and energy losses during 2 years with considering the constraints of bus voltages and the current carrying capacity of conductors. The obtained results confirmed the effectiveness of the proposed method.

7. References

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